

Understand the concept of a linear or exponential function and use function notation. Recognize arithmetic and geometric sequences as examples of linear and exponential functions (F.IF.1-3)	
<b>Standard I.F.IF.1:</b> Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If $f$ is a function and $x$ is an element of its domain, then $f(x)$ denotes the output of $f$ corresponding to the input $x$ . The graph of $f$ is the graph of the equation $y=f(x)$ .	
Concepts and Skills to Master	
<ul style="list-style-type: none"> <li>• Understand the definition of a function in terms of mapping elements from one set (domain) to another set (range).</li> <li>• Explain how a given representation of a function (graph, table, equation, context, geometric model) can be used to identify elements of the domain and corresponding elements of the range (<math>x, f(x)</math>).</li> <li>• Understand the graph of <math>f</math> is the graph of the equation <math>y=f(x)</math>.</li> </ul>	
Related Standards: Current Course	Related Standards: Future Courses
All function standards (functions are used throughout high school mathematics courses), <a href="#">I.A.REI.10</a> , <a href="#">I.F.IF.5</a>	All function standards (functions are used throughout high school mathematics courses)

## Support for Teachers

Critical Background Knowledge
<ul style="list-style-type: none"> <li>• A function is a rule that assigns to each input exactly one output (<a href="#">8.F.1</a>)</li> <li>• Multiple representations (tables, graphs, equations, context, geometric models) (<a href="#">8.F.2</a>)</li> </ul>
Academic Vocabulary
Domain, range, function, input, output, corresponding, set, element
Resources
<a href="http://www.uen.org/core/core.do?courseNum=5630#71625">Curriculum Resources</a> : <a href="http://www.uen.org/core/core.do?courseNum=5630#71625">http://www.uen.org/core/core.do?courseNum=5630#71625</a>

Understand the concept of a linear or exponential function and use function notation. Recognize arithmetic and geometric sequences as examples of linear and exponential functions (F.IF.1-3)	
<b>Standard I.F.IF.2:</b> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.	
Concepts and Skills to Master	
<ul style="list-style-type: none"> <li>• Use function notation</li> <li>• Evaluate functions, including functions created using arithmetic operations (example: <math>f(x) + g(x)</math> or <math>f(x) - g(x)</math>).</li> <li>• Interpret statements that use function notation in terms of a context (example: given a context, explain <math>f(5) = 12</math> )</li> </ul>	
Related Standards: Current Course	Related Standards: Future Courses
All function standards (function notation is used throughout high school mathematics courses)	All function standards (function notation is used throughout high school mathematics courses)

## Support for Teachers

Critical Background Knowledge
<ul style="list-style-type: none"> <li>• Evaluate expressions (<a href="#">6.EE.2c</a>)</li> </ul>
Academic Vocabulary
Function notation, evaluate, input, domain, output, range
Resources
<a href="http://www.uen.org/core/core.do?courseNum=5630#71625">Curriculum Resources</a> : <a href="http://www.uen.org/core/core.do?courseNum=5630#71625">http://www.uen.org/core/core.do?courseNum=5630#71625</a>

Understand the concept of a linear or exponential function and use function notation. Recognize arithmetic and geometric sequences as examples of linear and exponential functions (F.IF.1-3)	
<b>Standard I.F.IF.3:</b> Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. Recognize arithmetic and geometric sequences as examples of linear and exponential functions. <i>For example, the Fibonacci sequence is defined recursively by <math>f(0)=f(1)=1, f(n+1)=f(n)+f(n-1)</math> for <math>n \geq 1</math>.</i>	
Concepts and Skills to Master	
<ul style="list-style-type: none"> <li>Recognize that sequences are functions (recognize the domain is the number of the term and the range is the value of the term).</li> <li>Define and express a recursive sequence as a function.</li> <li>Recognize that a sequence has a domain which is a subset of integers.</li> </ul>	
Related Standards: Current Course	Related Standards: Future Courses
<a href="#">I.F.BF.1a</a> , <a href="#">I.F.BF.2</a> , <a href="#">I.F.LE.1</a> , <a href="#">I.F.LE.2</a>	<a href="#">II.F.BF.1a</a> , <a href="#">III.A.SSE.4</a>

Support for Teachers

Critical Background Knowledge
<ul style="list-style-type: none"> <li>Use function notation (<a href="#">I.F.IF.2</a>)</li> <li>Understand definition of function (<a href="#">8.F.1</a> and <a href="#">I.F.IF.1</a>)</li> <li>Recognize sequences (taught concurrently with <a href="#">I.F.BF.1</a>, <a href="#">I.F.BF.2</a>)</li> </ul>
Academic Vocabulary
Recursive, sequence, functions, domain, range, subset, term
Resources
<a href="http://www.uen.org/core/core.do?courseNum=5630#71625">Curriculum Resources</a> : <a href="http://www.uen.org/core/core.do?courseNum=5630#71625">http://www.uen.org/core/core.do?courseNum=5630#71625</a>

Interpret linear or exponential functions that arise in applications in terms of a context (F.IF.4-6)	
<b>Standard I.F.IF.4:</b> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. <i>Key features include intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; and end behavior.</i>	
Concepts and Skills to Master	
<ul style="list-style-type: none"> <li>Given a graph, identify key features including x- and y-intercepts; <i>intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; and end behavior.</i></li> <li>Given a table of values, identify key features such as x- and y-intercepts; <i>intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; and end behavior.</i></li> <li>Use key features to sketch a graph of the function.</li> <li>Use interval notation and symbols of inequality to communicate key features of graphs.</li> </ul>	
Related Standards: Current Course	Related Standards: Future Courses
<a href="#">I.F.IF.6</a> , <a href="#">I.F.IF.7</a> , <a href="#">F.IF.9</a> , <a href="#">I.F.LE.1</a> , <a href="#">I.F.LE.3</a>	<a href="#">II.F.IF.4</a> , <a href="#">II.F.IF.6</a> , <a href="#">II.F.IF.7</a> , <a href="#">II.F.IF.9</a> , <a href="#">II.F.LE.3</a> , <a href="#">III.F.IF.4</a> , <a href="#">III.F.IF.6</a> , <a href="#">III.F.IF.7</a>


## Support for Teachers

Critical Background Knowledge
<ul style="list-style-type: none"> <li>Ability to graph a linear (<a href="#">8.F.2</a>) or exponential function from a table or equation</li> </ul>
Academic Vocabulary
Increasing, decreasing, positive, negative, intervals, intercepts, interval notation, maximum, minimum, symmetry, and end behavior
Resources
<b>Curriculum Resources:</b> <a href="http://www.uen.org/core/core.do?courseNum=5630#71625">http://www.uen.org/core/core.do?courseNum=5630#71625</a>

Interpret linear or exponential functions that arise in applications in terms of a context (F.IF.4-6)	
<b>Standard I.F.IF.5:</b> Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. <i>For example, if the function <math>h(n)</math> gives the number of person-hours it takes to assemble <math>n</math> engines in a factory, then the positive integers would be an appropriate domain for the function.</i>	
Concepts and Skills to Master	
<ul style="list-style-type: none"> <li>Identify domain of a function from any representation.</li> <li>Relate the domain to context, explaining restrictions as a result of the context.</li> </ul>	
Related Standards: Current Course	Related Standards: Future Courses
<a href="#">I.A.CED.2</a> , All functions standards (domain is used throughout high school mathematics courses)	<a href="#">II.A.CED.2</a> , All functions standards (domain is used throughout high school mathematics courses)


Support for Teachers

Critical Background Knowledge
<ul style="list-style-type: none"> <li>Familiarity with function notation and domain (<a href="#">I.F.IF.2</a>)</li> <li>Understand the definition of function (<a href="#">8.F.1</a> and <a href="#">I.F.IF.1</a>)</li> <li>Independent, dependent variables and input/output (<a href="#">8.F.1</a>)</li> </ul>
Academic Vocabulary
Domain, function
Resources
<a href="http://www.uen.org/core/core.do?courseNum=5630#71625">Curriculum Resources</a> : <a href="http://www.uen.org/core/core.do?courseNum=5630#71625">http://www.uen.org/core/core.do?courseNum=5630#71625</a>

Interpret linear or exponential functions that arise in applications in terms of a context (F.IF.4-6)	
<b>Standard I.F.IF.6:</b> Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. 	
Concepts and Skills to Master	
<ul style="list-style-type: none"> <li>Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Focus on linear and exponential functions.</li> <li>Estimate the rate of change from a graph.</li> </ul>	
Related Standards: Current Course	Related Standards: Future Courses
<a href="#">I.F.IF.9</a> , <a href="#">I.F.LE.1</a> , <a href="#">I.F.LE.3</a> , <a href="#">I.S.ID.6</a> , <a href="#">I.S.ID.7</a>	<a href="#">II.F.IF.6</a> , <a href="#">II.F.IF.9</a> , <a href="#">II.F.LE.3</a> , <a href="#">III.F.IF.6</a> , <a href="#">III.F.IF.9</a> , <a href="#">III.F.LE.3</a>

## Support for Teachers

Critical Background Knowledge
<ul style="list-style-type: none"> <li>Determine the rate of change from a description of a relationship or from two (x,y) values and interpret its meaning (<a href="#">8.F.4</a>)</li> <li>Explain the slope <math>m</math> between any two points on a non-vertical line (<a href="#">8.EE.6</a>)</li> </ul>
Academic Vocabulary
Average rate of change, interval
Resources
<a href="http://www.uen.org/core/core.do?courseNum=5630#71625">Curriculum Resources</a> : <a href="http://www.uen.org/core/core.do?courseNum=5630#71625">http://www.uen.org/core/core.do?courseNum=5630#71625</a>

Analyze linear or exponential functions using different representations (F.IF.7,9)	
<p><b>Standard I.F.IF.7:</b> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. </p> <ul style="list-style-type: none"> <li>a. Graph linear functions and show intercepts.</li> <li>e. Graph exponential functions, showing intercepts and end behavior.</li> </ul>	
Concepts and Skills to Master	
<ul style="list-style-type: none"> <li>• Given an equation of a linear or exponential function, create a graph by hand and show key features (intercepts, end behavior).</li> <li>• Given an equation of a linear or exponential function, create a graph with technology and show key features (intercepts, end behavior).</li> </ul>	
Related Standards: Current Course	Related Standards: Future Courses
<a href="#">I.F.IF.4</a> , <a href="#">I.F.IF.5</a> , <a href="#">I.F.IF.6</a> , <a href="#">I.A.REI.6</a> , <a href="#">I.A.REI.11</a> , <a href="#">I.A.REI.12</a> , <a href="#">I.F.BF.3</a>	<a href="#">II.F.IF.4</a> , <a href="#">II.F.IF.7a, b</a> , <a href="#">III.F.IF.4</a> , <a href="#">III.F.IF.7b, c, d, e</a>

Support for Teachers

Critical Background Knowledge
<ul style="list-style-type: none"> <li>• Graph linear functions (<a href="#">8.EE.5</a>, <a href="#">8.F.3</a>, and <a href="#">8.F.5</a>)</li> </ul>
Academic Vocabulary
Linear, exponential, intercept, end behavior
Resources
<b>Curriculum Resources:</b> <a href="http://www.uen.org/core/core.do?courseNum=5630#71625">http://www.uen.org/core/core.do?courseNum=5630#71625</a>

Analyze linear or exponential functions using different representations (F.IF.7,9)	
<b>Standard I.F.IF.9:</b> Compare properties of two functions, each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). <i>Forexample, compare the growth of two linear functions, or two exponential functions such as <math>y=3^n</math> and <math>y=100 \cdot 2^n</math>.</i>	
Concepts and Skills to Master	
<ul style="list-style-type: none"> <li>• Compare properties of two functions, keeping the following in mind: <ul style="list-style-type: none"> <li>○ properties include rate of change, intercepts, end behavior</li> <li>○ function pairs include linear to linear, linear to exponential, exponential to exponential</li> <li>○ representations include algebraically, graphically, numerically in tables, or by verbal descriptions</li> </ul> </li> </ul>	
Related Standards: Current Course	Related Standards: Future Courses
<a href="#">I.F.IF.4</a> , <a href="#">I.F.IF.7</a> , <a href="#">I.F.LE.3</a> , <a href="#">I.S.ID.7</a>	<a href="#">II.F.IF.4</a> , <a href="#">II.F.IF.7</a> , <a href="#">II.F.LE.3</a> , <a href="#">III.F.IF.4</a> , <a href="#">III.F.IF.7</a> , <a href="#">III.F.LE.3</a>

## Support for Teachers

Critical Background Knowledge (Activating prior knowledge)
<ul style="list-style-type: none"> <li>• Compare properties of two functions (linear to linear), each represented in a different way (<a href="#">8.F.2</a>)</li> <li>• Interpret the equation of <math>y = mx+b</math> as defining a linear function (<a href="#">8.F.3</a>)</li> <li>• Construct a function, determine and interpret a rate of change and initial value of a linear function (<a href="#">8.F.4</a>)</li> <li>• Analyze graphs (increasing, decreasing, linear or nonlinear) (<a href="#">8.F.5</a>)</li> </ul>
Academic Vocabulary
function, slope, rate of change, intercept, interval, growth rate
Resources
<a href="http://www.uen.org/core/core.do?courseNum=5630#71625">Curriculum Resources</a> : <a href="http://www.uen.org/core/core.do?courseNum=5630#71625">http://www.uen.org/core/core.do?courseNum=5630#71625</a>